

3E1626

Roll No. _____

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B.Tech. III Semester (Main/Back) Examination, Dec. - 2016

Civil Engineering

3CE6A Advanced Engg. Mathematics

Time : 3 Hours

Maximum Marks : 80

Min. Passing Marks : 26

Instructions to Candidates:

Attempt any **five** questions, selecting **one** question from **each** unit. All questions carry **equal** marks. (Schematic diagrams must be shown wherever necessary. Any data you feel missing suitably be assumed and stated clearly. Units of quantities used/calculated must be stated clearly.

Unit - I

1. a) Find the Fourier series for the function $f(x) = \frac{x(\pi^2 - x^2)}{12}$ in $(-\pi, \pi)$
- b) Find the inverse z - transform of $\frac{1}{(z-5)^3}$ $|z| > 5$

OR

1. a) Find the Fourier series as for the second harmonic to represent the function given by table below :
- | | | | | | | | | | | | | |
|----------|-----------|------------|------------|------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| $x :$ | 0° | 30° | 60° | 90° | 120° | 150° | 180° | 210° | 240° | 270° | 300° | 330° |
| $f(x) :$ | 2.34 | 3.01 | 3.69 | 4.15 | 3.69 | 2.20 | 0.83 | 0.51 | 0.88 | 1.09 | 1.19 | 1.64 |
- b) Find the z- transform of $\{e^{-n} C_n\}$.

Unit - II

2. a) Using second shifting property find $L\langle f(t) \rangle$ where

$$f(t) = \begin{cases} \sin\left(t - \frac{\pi}{3}\right) & t > \frac{\pi}{3} \\ 0 & t < \frac{\pi}{3} \end{cases}$$

- b) i) Define unit step function (Heaviside's function) and find the Laplace transform of unit step function.

ii) Find $L^{-1}\left\{\frac{1}{s^2 + 8s + 16}\right\}$

OR

2. a) Prove $L\left\{\frac{\sin t}{t}\right\} = \tan^{-1} \frac{1}{s}$ and hence find $L\left\{\frac{\sin t}{t}\right\}$.

b) Solve $(D^2 + 9)y = \cos 2t$ where $y(0) = 1, y\left(\frac{\pi}{2}\right) = -1$.

Unit - III

3. a) Obtain the Fourier transform of

$$f(x) = \begin{cases} x^2 & |x| \leq 9 \\ 0 & |x| > 9 \end{cases}$$

b) Heat flow in an infinite bar with given initial temperature $u(x, t)$ is governed by

$$\frac{\partial u}{\partial t} = c^2 \frac{\partial^2 u}{\partial x^2}, t > 0, -\infty < x < \infty \text{ satisfy } u(x, 0) = f(x)$$

OR

3. a) Find the Fourier sine and cosine transform of $f(x) = e^{-x}, x \geq 0$ Also show that

$$\int_0^{\infty} \frac{x \sin mx}{x^2 + 1} dx = \frac{\pi}{2} e^{-m}, m > 0$$

b) Use the method of Fourier transform to determine the displacement $u(x, t)$ of an infinite string, given that the string is initially at rest and the initial displacement is $f(x), -\infty < x < \infty$. show that the solution can be put in the form

$$u(x, t) = \frac{1}{2} [f(x+(t)) + f(x-(t))]$$

Unit - IV

4. a) Evaluate

1) $\Delta \log x$

2) $\Delta - \nabla = \Delta \nabla$

b) The population of a country in the decadal censuses were as under estimate the population for the year 1925

year (x):	1891	1901	1911	1921	1931
Population (in thousands) f(x):	46	66	81	93	101

OR

4. a) Evaluate $\int_0^1 \frac{dx}{1+x}$ by using

i) Simpson's 1/3

ii) Simpson's 3/8

Trapezoidal method

b) Find the value of $f(5)$ with the help of Lagrange's interpolation formula. Given that

x	0	2	3	4	7
f(x)	2	4	8	16	128

Unit - V

5. a) Use Euler's modified method with one step to obtain the value of y at $x=0.1$

when $\frac{dy}{dx} = x^2 + y$ with $x = 0, y = 0.94$

b) Use Runge - Kutta fourth order method to solve

$\frac{dy}{dx} = -2xy^2, y(0) = 1$ with $h = 0.2$ for $x = 0.2$ and 0.4

OR

5. a) Use Milne's predictor - corrector method to obtain $y(0.4)$ for the following differential Equation. $\frac{dy}{dx} = 2e^x - y$ given that

x	0	0.1	0.2	0.3
y	2	2.01	2.04	2.09

b) Apply Picard's method to find the solution of the differential equation

$\frac{dy}{dx} = y - x$ with $x = 0, y = 2$ up to third order of approximation.

