

**5E5021**

Roll No. \_\_\_\_\_

Total No of Pages: **4****5E5021**

**B. Tech. V Sem. (Main / Back) Exam., Dec. 2014**  
**Electronics and Communication Engineering**  
**5EC1A Signal & Systems**  
**(Common for EC, EI)**

**Time: 3 Hours****Maximum Marks: 80**  
**Min. Passing Marks: 24***Instructions to Candidates:*

Attempt any **five questions**, selecting **one question from each unit**. All questions carry **equal marks**. Schematic diagrams must be shown wherever necessary. Any data you feel missing suitably be assumed and stated clearly.

Units of quantities used/calculated must be stated clearly.

Use of following supporting material is permitted during examination.

(Mentioned in form No. 205)

1. NIL2. NIL**UNIT - I**Q. 1 (a) Given  $x(t) = t.u(t)$ ,  $y(t) = u(t).t^2$ . Plot -

(i)  $w(t) = x(t) + y(t)$

(ii)  $g(t) = x(t) - y(t)$

(iii)  $f(t) = y(t) - x(t)$

(iv)  $z(t) = x(t) y(t)$

**[8]**

- (b) The output of a system is defined by  $y[n] = w[n] \times x[n]$ .  $x[n]$  is the input signal and  $w[n]$  is a function of  $n$ . Determine the properties of the system. [8]

**OR**

- (a) Given  $y[n] = \cos(5t) \cdot x(t)$ . Determine the properties of the system. [8]
- (b) Consider the impulse response of a discrete LTI system to be

$$h[n] = \frac{1}{3}; \quad 0 \leq n \leq 4$$
$$= 0; \quad \text{otherwise}$$

Find an expression that relates an arbitrary input  $x[n]$  to the output  $y[n]$ . [8]

**UNIT-II**

- Q. 2 (a) Determine the Fourier series coefficients for the signal  $x(t)$  given as

$$x(t) = \cos 4t + \sin 8t + 3 \quad [8]$$

- (b) Write down the properties of fourier series. [8]

**OR**

- (a) Find the average power of the signal  $x(t) = 2 + 2 \cos 4t$ . [8]

- (b) Obtain the time domain periodic signal  $x(n)$ , given  $x(k)$  as [8]

$$x[k] = \cos\left(\frac{6\pi}{17}k\right)$$

### UNIT- III

Q. 3 (a) Find the Fourier Transform (FT) of the unit step function [8]

$$x(t) = \begin{cases} 1, & t \geq 0 \\ 0, & t < 0 \end{cases}$$

(b) Use partial fraction expansion and linearity to determine the inverse FT of

$$x(j\omega) = \frac{-j\omega}{(j\omega)^2 + 3j\omega + 2} \quad [8]$$

OR

(a) Find the FT of the signal  $x(t) = e^{-at} \cos \omega_0 t \cdot u(t)$ ,  $a > 0$ . [8]

(b) Use the modulation property to find the FT of  $\sin^2(2t)$ . [8]

$$x(t) = \frac{4}{\pi^2 t^2} \sin^2(2t)$$

### UNIT-IV

Q. 4 (a) Find the Z-transform and ROC of  $x[n] = \alpha^{|n|}$ , [8]

(b) Write down the properties of z-transform. [8]

OR

(a) Find z-transform and ROC of the signal -

$$x[n] = \{4(3)^n - 3(5)^n\} u(n). \quad [8]$$

(b) Find inverse z- transform of

[8]

$$x(z) = \frac{z-4}{z^2-5z+6}; |z| > 3$$

### UNIT-V

Q. 5 Consider the continuous -time signal

$$x(t) = \cos(100\pi t)$$

- (a) Determine the minimum sampling rate required to avoid aliasing.
- (b) Suppose that the signal is sampled at the rate  $f_s = 200\text{Hz}$ , what is the discrete-time signal obtained after sampling?
- (c) Suppose that the signal is sampled at the rate  $f_s = 75\text{ Hz}$ , what is the discrete-time signal obtained after sampling?
- (d) What is the frequency  $0 < f < f_s/2$  of a sinusoid that yields samples identical to those obtained in part (c)? [4×4=16]

OR

(a) Let  $x(n) = \{3, 4, 5, 6\}$

(i) Find  $g(n) = x(2n-1)$  and the step interpolated signal  $h(n) = x(0.5n-1)$ .

(ii) Find  $y(n) = x(2n/3)$  assuming step interpolation where needed. [8]

(b) A signal  $x(t) = \sin(\pi t)/\pi t$  is sampled by  $s(t) = \sum_{n=-\infty}^{\infty} \delta(t - n/2)$ . [8]

Determine and sketch the sampled signal and its Fourier transform.